

Complex structures of dense lithium: electronic origin

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Outline

- Main factors of crystal structure stability
Concept of the Fermi Sphere - Brillouin Zone interaction: Cu-Zn alloy system
- Lithium – the simplest metal under pressure: structural complexity
- Core ionization: increase of the valence electron number

Alkali metals under pressure: structural transformations

Li	7.5 bcc	39 fcc	42 <i>hR1</i>	60 <i>cI16</i>	70 <i>oC88</i>	95 <i>oC40</i>	<i>oC24</i>	< 125 GPa
Na	65 bcc	104 fcc	117 <i>cI16</i>	125 <i>oP8</i>	180 h-g (<i>tI19*</i>)	<i>hP4</i>	< 200 GPa	
K	11.6 bcc	20 fcc	25 <i>hP4</i>	35 <i>h-g (tI19*)</i>	54 <i>oP8</i>	90 <i>tI4</i>	96 <i>oC16</i>	< 112 GPa
Rb	7 bcc	13 fcc	17 <i>oC52</i>	20 h-g (<i>tI19*</i>)	48 <i>tI4</i>	<i>oC16</i>	< 70 GPa	
Cs	2.4 bcc	4.2 fcc	4.3 <i>oC84</i>	12 <i>tI4</i>	72 <i>oC16</i>	<i>dhcp</i>	< 223 GPa	



s-d electron transfer

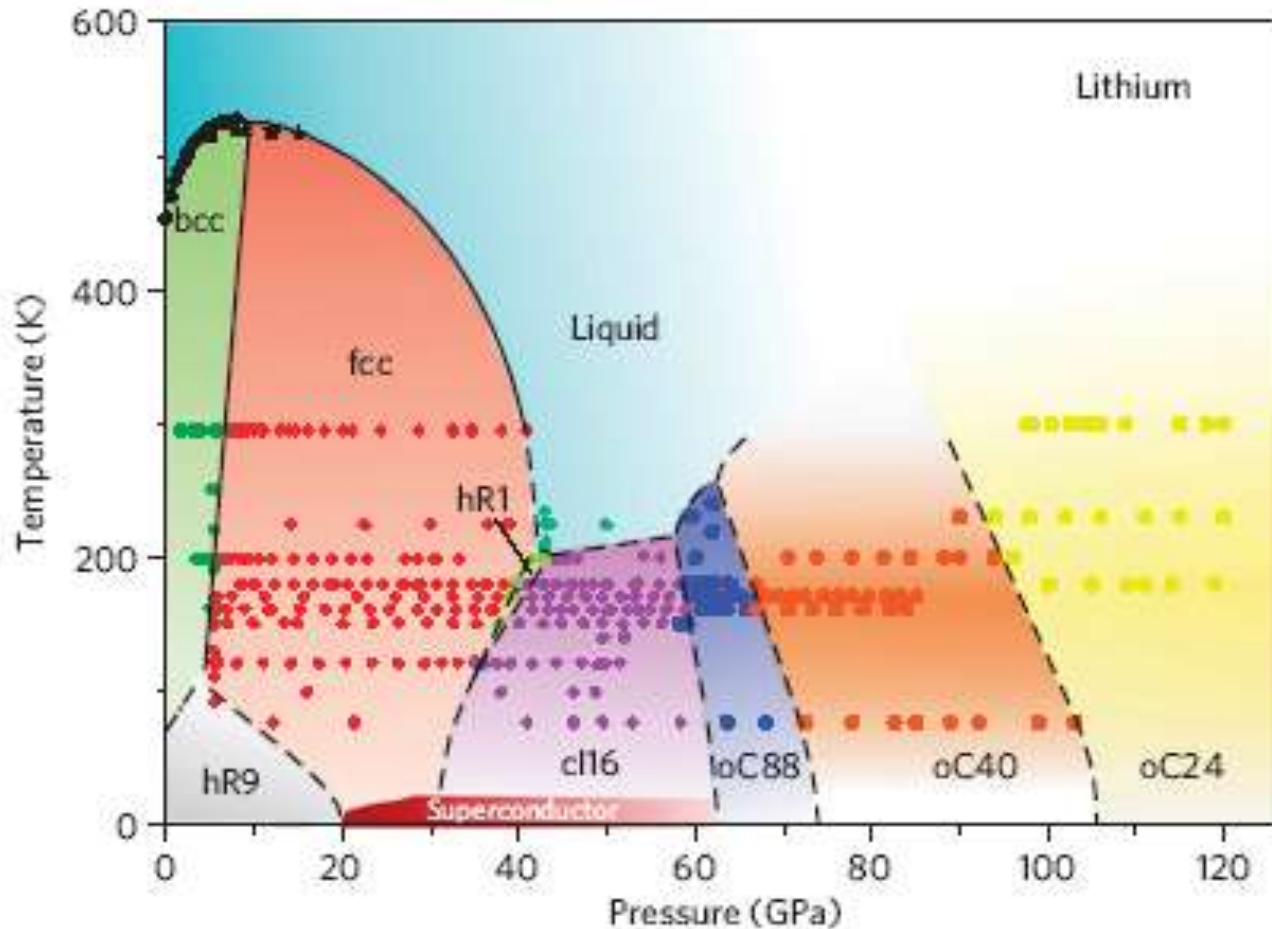


core ionisation

Large arrows indicate supposed core ionization

(at compression V/V_0 equal 0.35 for Li, 0.24 for Na, 0.33 for K, 0.31 for Rb and 0.43 for Cs).

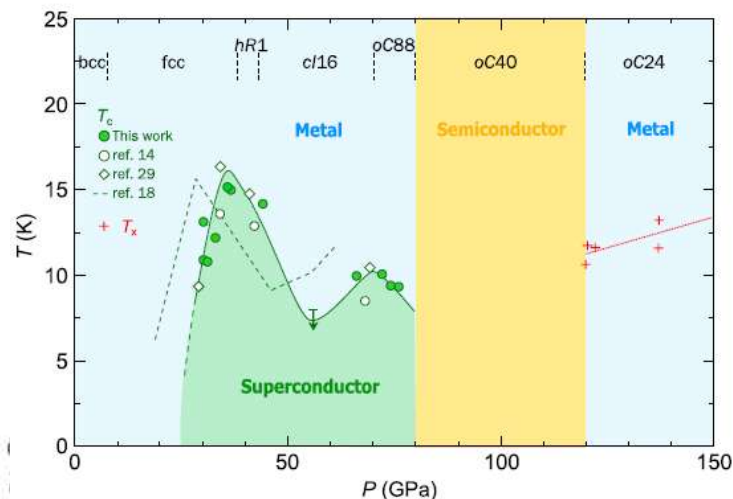
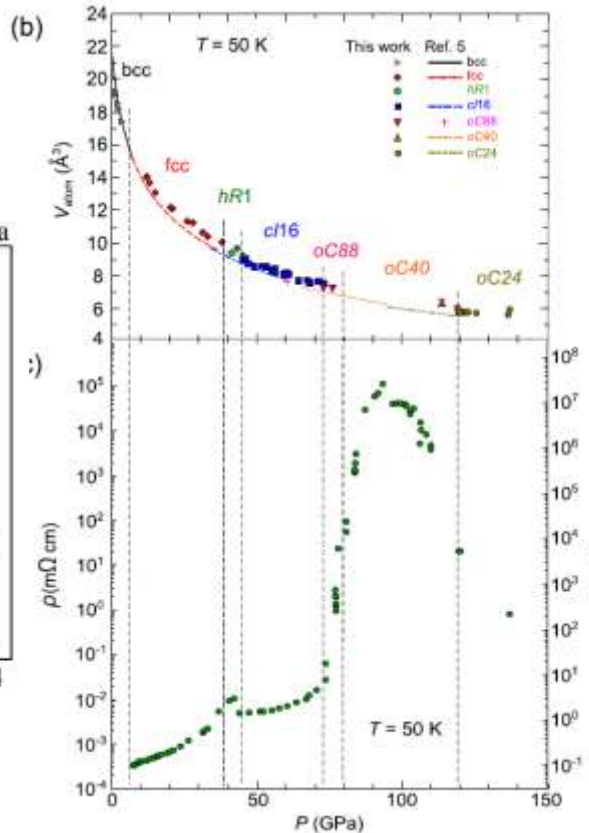
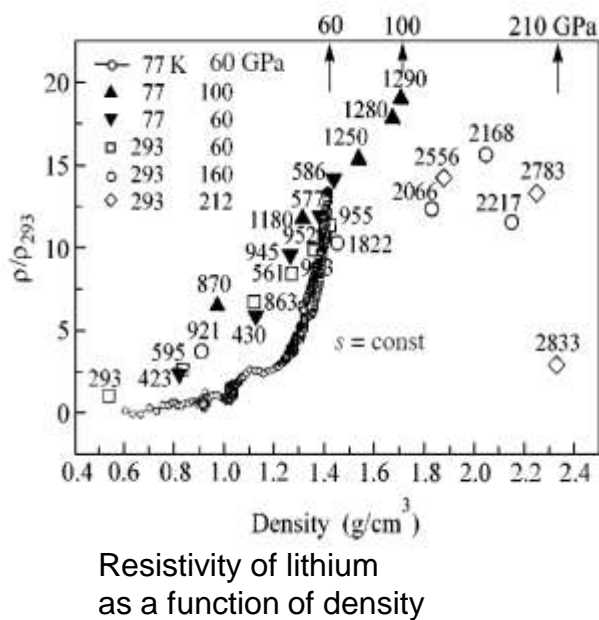
Melting curve of the lightest alkali metal: lithium



[Guillaume C, Gregoryanz E, Degtyareva O, et al. *Nature Physics* (2011) 7, 211]

Anomalous Resistivity of Lithium at High Dynamic Pressure

Pressure-induced reentrant metallic phase in lithium



The superconducting transition temperature T_c as functions of pressure and resistivity drops T_x

V.E.Fortov, V.V.Yakushev,
K.L.Kagan, I.V. Lomonosov, et al.
[JETP Lett. 74, 418 \(2001\)](#)

Matsuoka T, Sakata M, Nakamoto Y, et al.
[Phys.Rev.B 89, 144103 \(2014\)](#)

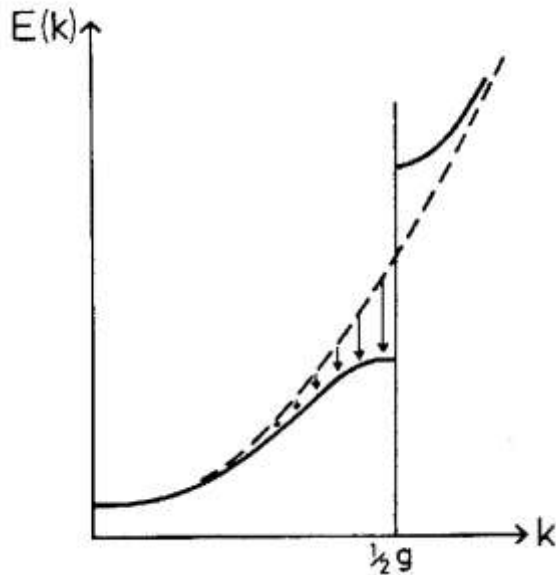
Main factors of phase stability

$$E = E_0 + E_{Ewald} + E_{BS}$$

The crystal energy consists of two terms
electrostatic and electronic band structure

$$E_{Ewald} = -\alpha \frac{(Ze)^2}{2r_0}$$

$$E_{BS} = \sum_q |S(q)|^2 \Phi(q)$$



Band structure energy E_{BS}

Volume scaling:

$$\sim V^{-1/3}$$

$$\sim V^{-2/3}$$

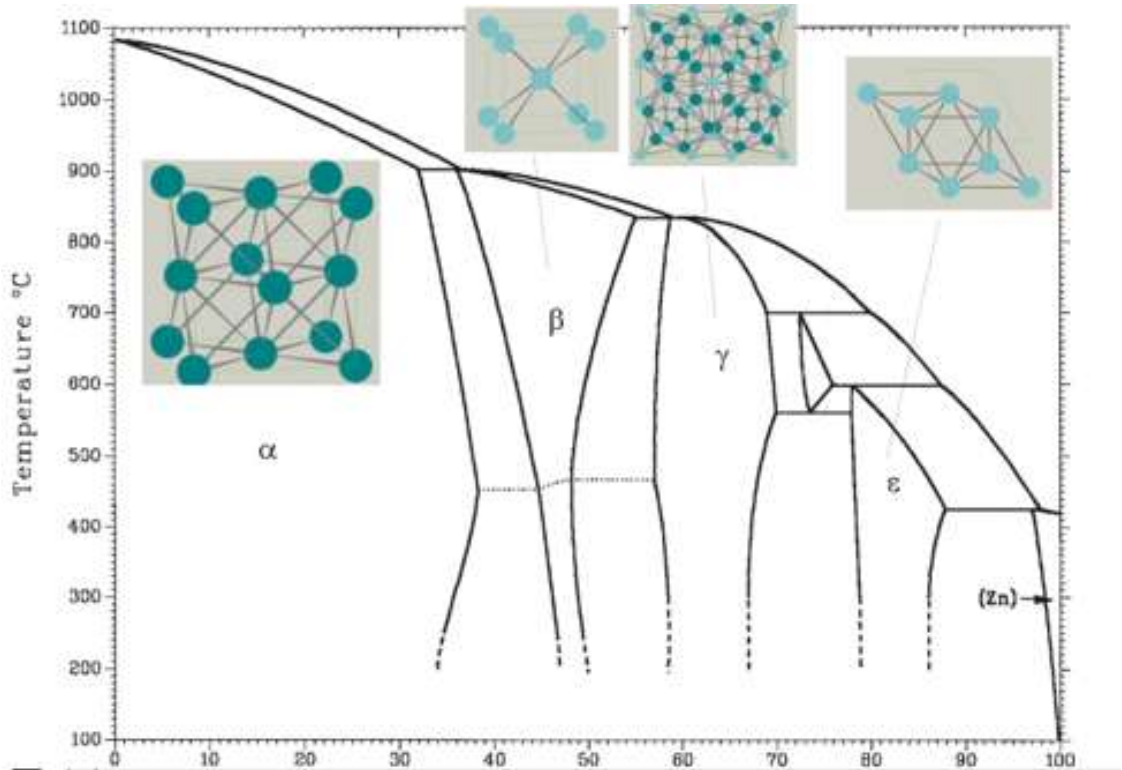
Enhancement of the Hume-Rothery
arguments at compression

The brass alloy Cu-Zn system



The Age of Bronze

A. Rodin

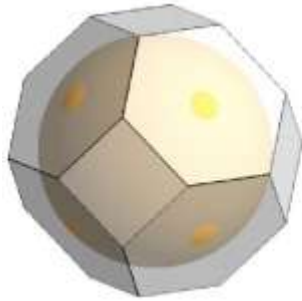


α (fcc) \rightarrow β (bcc) \rightarrow γ (complex cubic) \rightarrow ϵ (hcp)
1.35 \rightarrow 1.5 \rightarrow 1.62 \rightarrow 1.75 electron/
atom

Massalsky (1996)

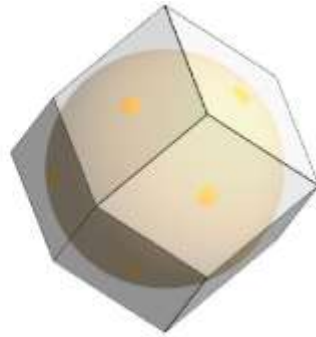
Hume-Rothery phases: Fermi sphere – Brillouin zone interaction

α (fcc) - phase



{111}
{200}

β (bcc) - phase



{110}

γ - complex cubic



{411}
{330}

ϵ (hcp) - phase



{002}
{101}

Fermi sphere – energy surface of free valence electrons, radius $k_F = \left(\frac{3\pi^2 z}{V} \right)^{1/3}$

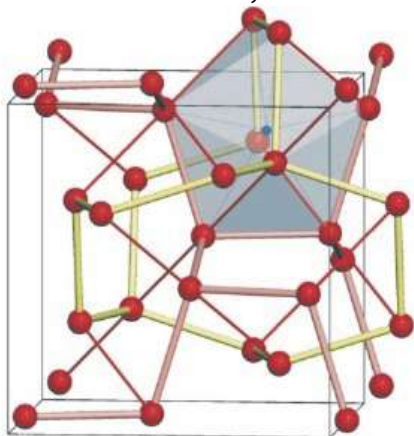
Brillouin zone – planes in reciprocal space with vector $q_{hkl} = \frac{2\pi}{d_{hkl}}$

Interaction (condition of phase stability): $k_F \approx \frac{1}{2} q_{hkl}$

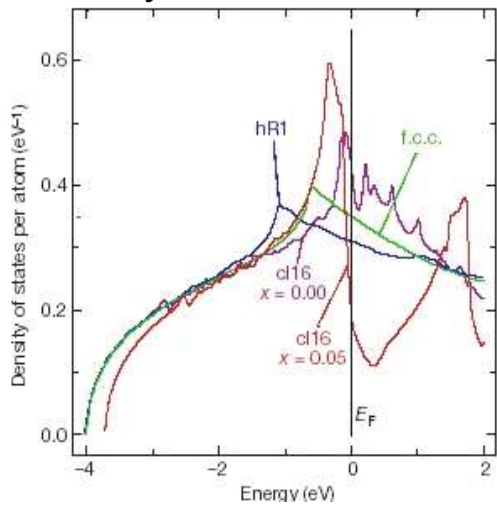
Alkali metals: pressure induced complexity

Li-c/16 at 46 GPa

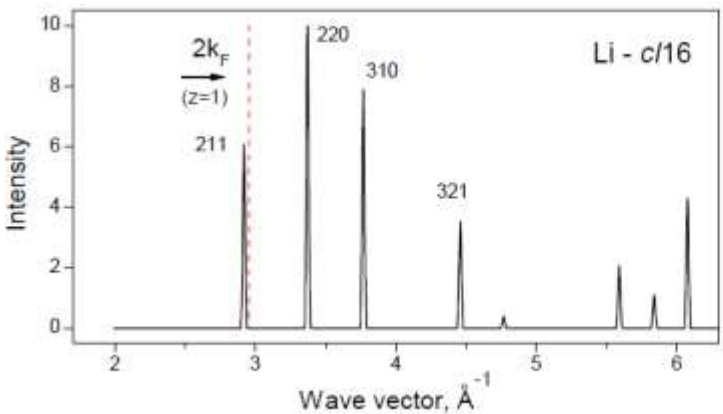
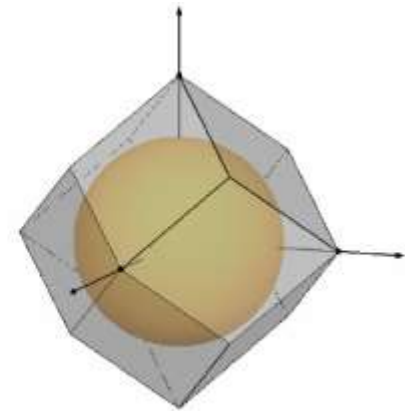
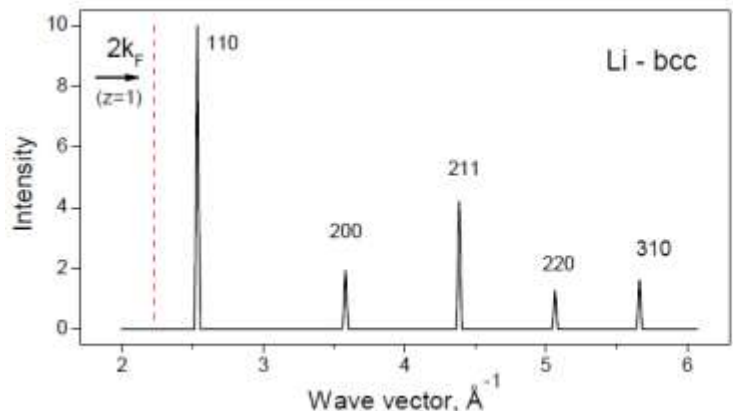
(Hanfland et al, Nature 2000)



Crystal structure



Electron density of states



$$V_{FS}/V_{BZ} \sim 0.90$$

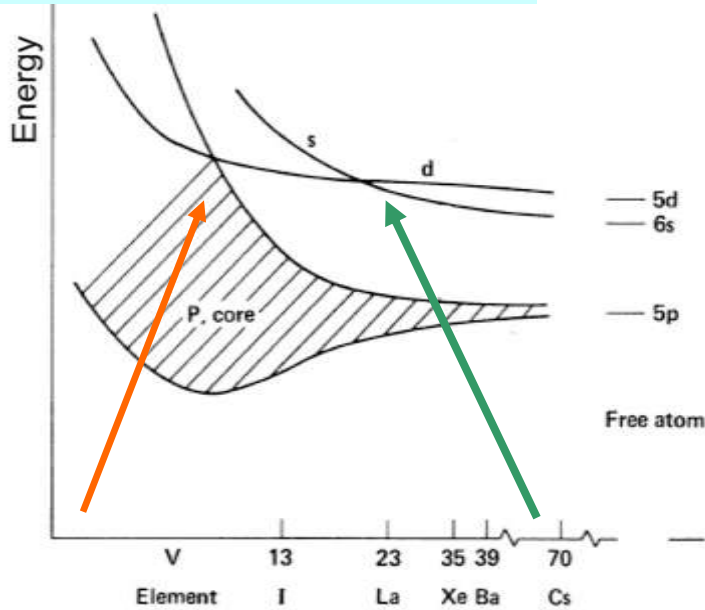
Brillouin zone Li-c/16

(V Degtyareva 2003)

Electronic energy levels

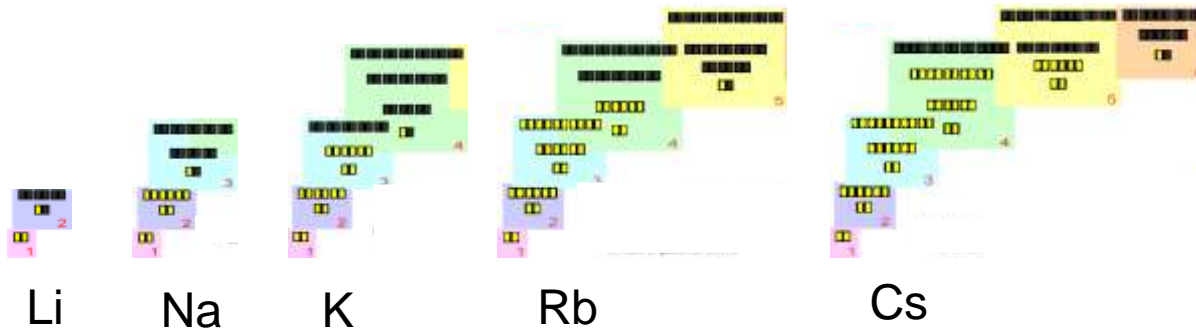
vs atomic volume

Ross & McMahan, *Phys. Rev. B*
26, 4088 (1982)



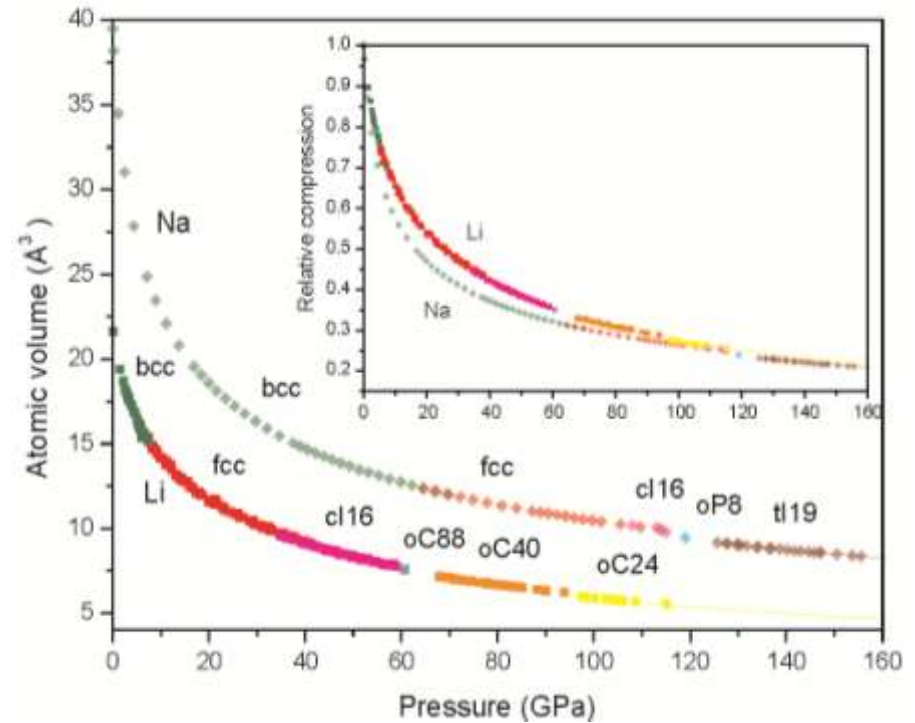
*s-d-p(core)
hybridization*

s-d transfer



Equations of state of Li and Na

Inset: relative compression V/V_0

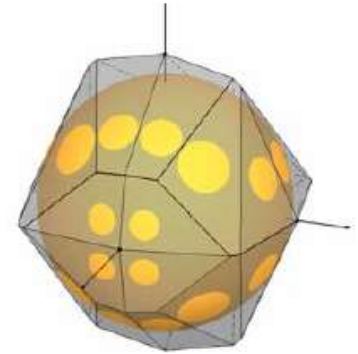
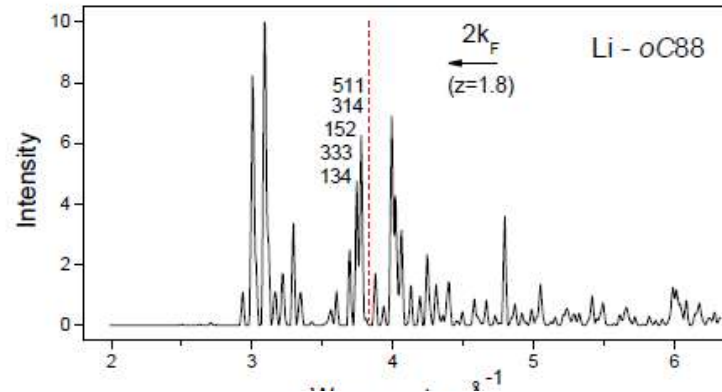


[Guillaume C, Gregoryanz E, Degtyareva O, et al.
Nature Physics (2011) 7, 211]

Complex semiconducting phases of Lithium above 60 GPa

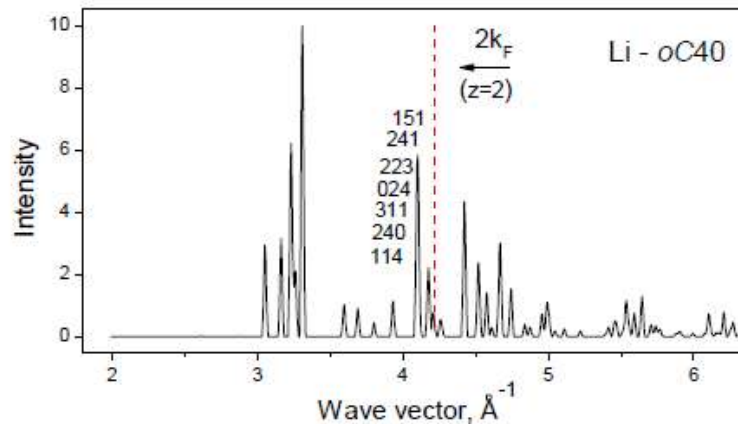
Li-*oC88* *C2mb* P= 61 GPa
 $a=8.569\text{\AA}$, $b=9.282\text{\AA}$, $c =8.389\text{\AA}$

$$V_{\text{FS}}/V_{\text{BZ}} = 0.90$$



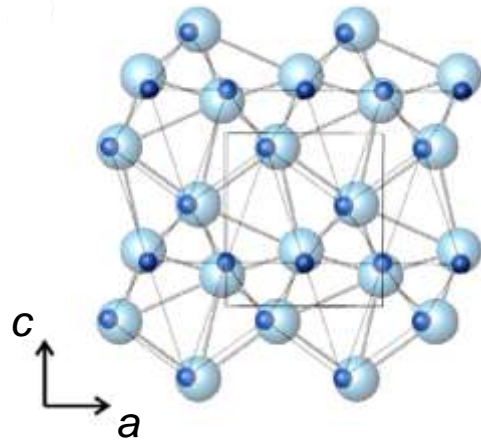
Li-*oC40* *C2cb* P= 90 GPa
 $a=4.815\text{\AA}$, $b=7.948\text{\AA}$, $c =6.613\text{\AA}$

$$V_{\text{FS}}/V_{\text{BZ}} = 0.96$$



For *post-cI16* phases with compression $V/V_0 > 0.35$ we suggest an overlap of valence and core electron levels with increase of effective valence electron numbers. This allows understanding semiconducting properties of *oC88* and *oC40* phases as filling of BZ by electron states and returning *oP24* to metal.

oP8 structure in Na and K: 2 valence electrons



Na-*oP8* *Pnma*

$P = 119 \text{ GPa}$ [1]

$a = 4.765 \text{ \AA}$, $b = 3.020 \text{ \AA}$,

$c = 5.251 \text{ \AA}$

Recently found the *oP8* structure in Na and K [1,2]
Is considered as a Hume-Rothery phase
assuming alkali elements as **divalent** metals [3]

[1] Gregoryanz E et al., Science 320, 1054 2008

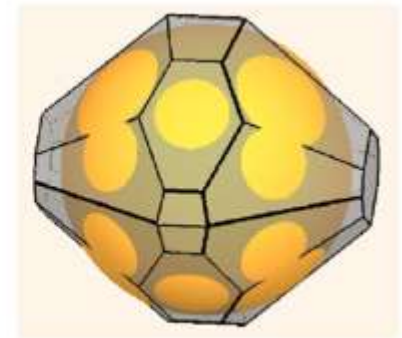
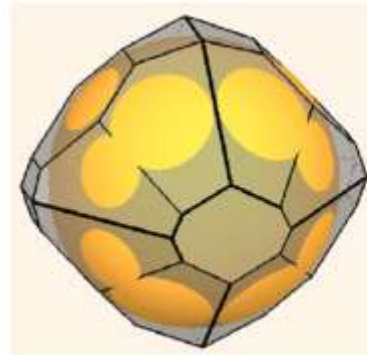
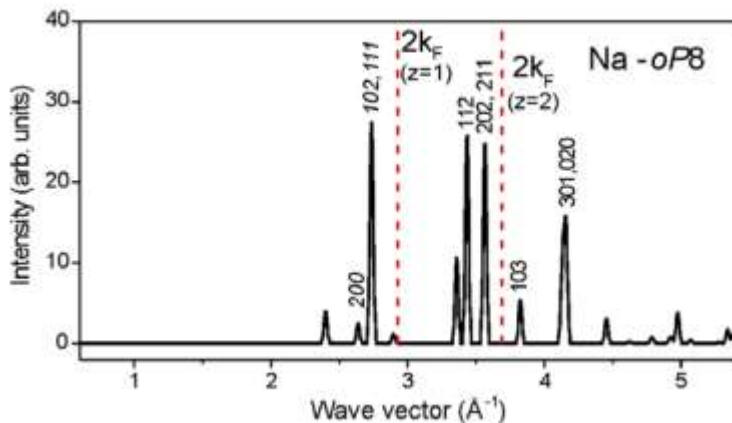
[2] Lundegaard L F et al., Phys Rev B 80, 020101 2009

[3] Degtyareva V F & Degtyareva O, New J Phys 11, 063037 2009

Brillouin zone of Na – *oP8* with the inscribed FS

The position of $2k_F$ for $z = 1$ and $z = 2$ for Na,
calculated from the free-electron model, is shown [3].

The structure and the form of BZ is similar to
AuGa compound ($z=2$)

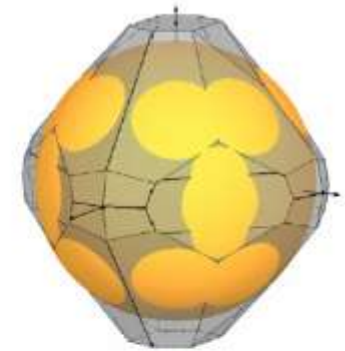
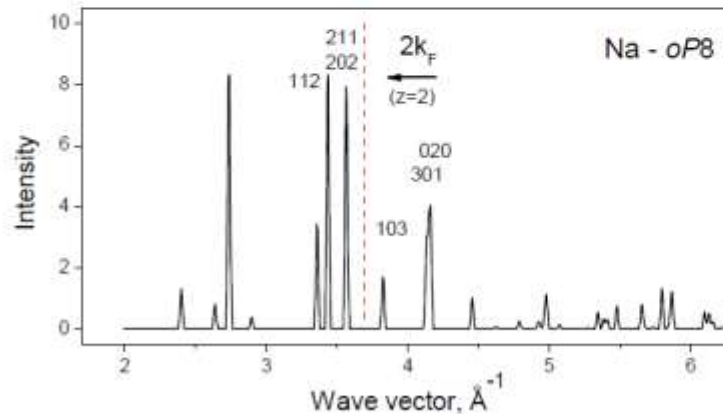
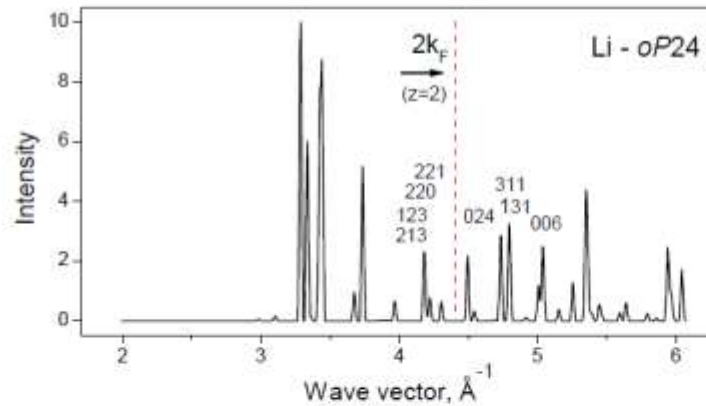


Li-*oP24* and Na-*oP8* structural relation

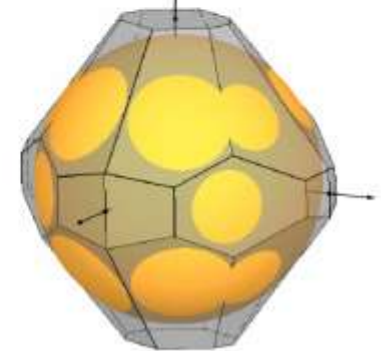
Li-*oP24* *Pbca* P= 115 GPa
 $a=4.213\text{\AA}$, $b=4.205$, $c =7.482\text{\AA}$

Na-*oP8* *Pnma* P= 119 GPa
 $a =4.765\text{\AA}$, $b=3.020\text{\AA}$, $c=5.251\text{\AA}$

(Gregoryanz et al., Science 320 1054, 2008)
 BZ projection is $\uparrow b^*$, $\rightarrow a^*$, down c^*



$$V_{FS}/V_{BZ} = 0.93$$



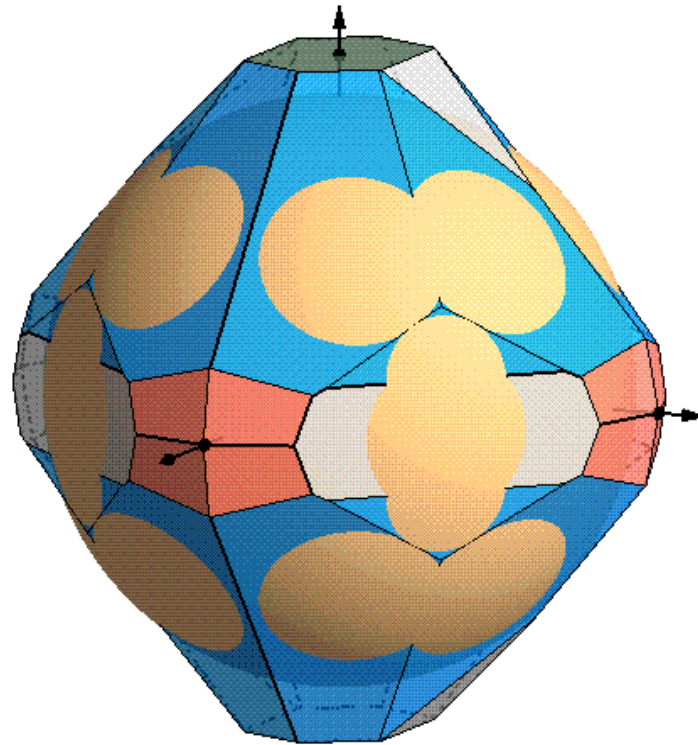
Li-*oP24* and Na-*oP8* are related to AuGa-*oP8* and to hexagonal NiAs-*hP4*.

Cell parameters for Na-*oP8* are related to c_h , a_h , $a_h\sqrt{3}$,
 for Li-*oP24* are related to $a_h\sqrt{3}$, c_h , $3a_h$.

BZ configurations are similar for both phases.

Valence electron number $z = 2$ is assumed for Li-*oP24* as in Na-*oP8* and AuGa-*oP8* phases.

Li – $oP24$



Conclusions

- Crystal structures of simple metals under pressure are determined by valence electron energy term
- Fermi sphere - Brillouin zone interactions favour the low-symmetry structures with BZ planes close to the FS by the Hume-Rothery mechanism
- Formation of low-packing structures is related to the core ionization
- Melting curve with maximum and negative slope in alkali metals is defined by Hume-Rothery effect

Thanks for attention

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